Research Paper

Analysis of Electric Field and Thickness of Undoped-GaSb Single-Layer Samples using Photoreflectance Measurement

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Abstract

The purpose of this study is twofold: (1) to grow undoped-GaSb epitaxial structure on a high concentration \(n^+\)-GaSb substrate by molecular beam epitaxy and (2) to analyze the grown undoped-GaSb epitaxial structure through photoreflectance (PR) measurements. PR spectrum analysis of the undoped-GaSb epitaxial layer at room temperature shows three notable features. First, in the region above the fundamental band gap \(E_g\), the Franz-Keldysh oscillation (FKO) makes the PR signals oscillate. Second, low electric field PR is observed near \(E_g\). Third, low energetic interference oscillations (LEIOs) occur in the region below the bandgap. An electric field is formed on the surface of the undoped-GaSb layer (i.e., in the interface between the undoped-GaSb and air); by using the FKO component, the calculated magnitude is 70 kV/cm at a growth temperature of 485 °C. In addition, the analysis of the FKO and low electric field PR data indicate a fundamental band gap \(E_g\) of 0.723 eV. The thickness of the undoped-GaSb epi-layer, calculated using the LEIO PR spectrum, is 1040 nm.

Keywords: Molecular beam epitaxy, Photoreflectance, GaSb

I. Introduction

Modulation spectroscopy is the application of external modulation to measure the optical spectrum of a sample. It is based on changes in the internal or surface electric field of the sample. The optical spectrum measured by modulation spectroscopy has differential characteristics of the perturbation parameter and the reflectivity of the sample. Therefore, the reflectance is highly sensitive to the variation of the perturbation parameter. Accordingly, modulation techniques can be divided into electroreflectance (ER) spectroscopy (direct field modulation) and light-reflectance or photoreflectance (PR) modulation (indirect field modulation) [1]. ER was first studied by Seraphin [2], and Wang et al. [3] developed PR as a non-destructive method.

In the case of PR, the energy of the pump light that is periodically incident is higher than the bandgap energy of the sample in order to generate a carrier. After absorbing the light, the electron-hole pairs in the sample are separated by the internal electric field, which is then reduced [4]. The variation of the electric field causes the band bending of the sample. The optical properties of the material, such as the reflectance, change with the dielectric function. Therefore, the characteristics of the sample can be analyzed by PR measurements.

In this study, undoped-GaSb epitaxial layers were grown on a high concentration \(n^+\)-GaSb substrate \((n\approx 10^{18} \text{ cm}^{-3})\) by molecular beam epitaxy (MBE) at a growth temperature of 485 °C and the PR spectra were measured. The PR spectra were analyzed theoretically and from them the magnitude of the electric field and the thickness of the thin film were obtained. The PR theory, which is applied to the single layer semiconductor, is introduced with respect to the magnitude of the electric field. The low energy interference oscillation (LEIO) [5-7], which is caused by the interference between the reflection off the surface and the PR signal from the substrate, is considered at energies lower than the band gap energy. The fabrication process and structure of the GaSb thin film according to the growth temperature are explained, as well as the PR experimental conditions. Finally, the results of the electric field magnitude, thin film thickness, and medium information (effective mass) obtained from experiments and cal-

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culations are summarized.

II. Theory

The optical properties of the medium are indicated by the complex dielectric function. When light modulation is applied to the medium, the change in reflectance is related to the real and imaginary parts of the complex dielectric function. Seraphin and Bottka [8] express the relative change of reflectance as:

$$\frac{\Delta R}{R} = a\Delta e_1 + b\Delta e_2,$$

(1)

where $\Delta R = R_{\text{eff}} - R_{\text{ni}}$, $R = R_{\text{eff}}$, $\Delta e = \Delta e_1 + i\Delta e_2$, is the change in the dielectric function, and $a$ and $b$ are the Seraphin coefficients [8] given by the refractive index $n$ and the extinction coefficient $k$ of the semiconductor, respectively. In general, the imaginary part of the Seraphin coefficient below the band gap can be neglected because the light absorption is very small. According to Aspnes [9], if the electric field is applied to the semiconductor medium, the electro-optic energy of the charged particles is determined as:

$$\hbar\theta = \left(\frac{eF}{\sqrt{2}\mu}\right)^{2/3},$$

(2)

where $F$ is the electric field strength, $\mu$ is the interband reduced effective mass, $\hbar = h/2\pi$, where $h$ is the Planck constant, and $e$ is the electron charge.

Comparing the phenomenological lifetime broadening parameter $\Gamma$ with the electro-optic energy proposed by Aspnes, the electric field formed inside the sample can be classified into three categories: low, medium, and high [9].

i) Low field region ($\hbar\theta < \Gamma$)

Assuming a uniform broadening parameter, the dielectric function has a generalized Lorentzian shape, and the change in reflectance is expressed in the low electric field region as [10]:

$$\frac{\Delta R}{R} = \text{Re}[C\exp(\phi(E - E_\text{cp} + i\Gamma_\text{cp})^{-m})],$$

(3)

where $C$ is an amplitude parameter, $E = \hbar\omega$ is the photon energy, $E_\text{cp}$ is the critical point energy, $\phi$ is the phase parameter, and $m=2,2.5$, and 3 represent the exciton transition, the three-dimensional (3D) band-to-band transition, and the two-dimensional (2D) band-to-band transition, respectively. In this study, the exciton and 2D third differential functional form (TDFF), i.e., $m=2.5$, is used to analyze the energy states of the medium.

ii) Medium field region ($\hbar\theta \geq \Gamma$)

In the intermediate field region, the dielectric function represents the Franz-Keldysh oscillation (FKO) [1]. The Franz-Keldysh effect is represented by Airy functions and the change in the dielectric function can be expressed as [11]

$$\Delta e_1 = B_0 \cdot \sqrt{i\theta} \cdot \frac{H(\eta)}{(E - i\Gamma)^2},$$

(4a)

$$\Delta e_2 = B_0 \cdot \sqrt{i\theta} \cdot \frac{k(\eta)}{(E - i\Gamma)^2},$$

(4b)

$$H(\eta) = \pi[\eta(Ai' - \eta Ai'')^2] + j\pi[\eta Ai' Bi' - \eta Ai' Bi] + j\sqrt{\eta},$$

(4c)

where $B_0$ is a constant related to the polarization and transition strengths, $\eta = (E - \eta)/((\hbar\theta))$, $Ai(x)$ and $Bi(x)$ are Airy functions of the first and second kinds, respectively, $Ai'(x)$ and $Bi'(x)$ are differential forms of $Ai(x)$ and $Bi(x)$, respectively, $E_\eta$ is the transition energy, and $\eta(x)$ is a unit step function. Furthermore, transitions involving degenerated valence bands should be considered separately by replacing $\mu$ by $\mu_{hh}$ and $\mu_{hh}$, which correspond to transitions including the light and heavy hole, respectively. This creates nesting in the PR spectra using Eqs. (1) and (4) as:

$$\frac{\Delta R}{R} = A_{hh} \left(\frac{\Delta R}{R}\right)_{hh} + A_{hh} \left(\frac{\Delta R}{R}\right)_{hh},$$

(5)

where $A_{hh}$ and $A_{hh}$ are the relative amplitudes of the heavy and light hole transitions, respectively. As shown in Eq. (5), the exact form of $\Delta R/R$ in the intermediate electric field region is quite complex. Thus, Aspnes and Studna derived simple expressions as follows [12]:

$$\frac{\Delta R}{R} = \cos(2\pi f(E - E_\eta)^{3/2} + \chi),$$

(6a)
where the value of Eq. (6b) represents the frequency when Fourier transform is applied to the signal of the intermediate PR, the value of Eq. (6c) is equal to the position of \( n \)-th maximum or minimum, and \( \chi \) is an arbitrary phase factor.

Figure 1 shows the theoretical PR spectra in the intermediate electric field region in the GaSb sample structure. Because the transitions in the valence band assume heavy holes and light holes, the PR equation requires two Airy functions. GaSb has \( \phi = 0.726 \text{ eV} \), \( F_{\phi} = 5 \text{ meV} \), \( m_{hh} = 0.65 m_0 \), \( m_{lh} = 0.041 m_0 \), and \( A_{hh}/ A_{lh} = 0.3 \), where \( m_{hh}, m_{lh}, m_e \), and \( m_e \) represent heavy hole’s, light hole’s, and electron’s effective mass and the free electron’s mass, respectively.

\[
f = \frac{2}{3\pi} \frac{\sqrt{2\mu}}{e HF}, \tag{6b}
\]

\[
n\pi = \frac{4}{3} \frac{(E_0 - E_n)^{3/2}}{(h\theta)^{3/2}} + \chi, \tag{6c}
\]

where the value of Eq. (6b) represents the frequency when Fourier transform is applied to the signal of the intermediate PR, the value of Eq. (6c) is equal to the position of \( n \)-th maximum or minimum, and \( \chi \) is an arbitrary phase factor.

Figure 1 shows the theoretical PR spectra in the intermediate electric field region in the GaSb sample structure. Because the transitions in the valence band assume heavy holes and light holes, the PR equation requires two Airy functions. GaSb has \( E_0 = 0.726 \text{ eV} \) at 300 K and used the amplitude ratio 0.30 (i.e., \( A_{hh}/ A_{hh} = 0.30 \)).

**iii) Low energetic interference oscillation (LEIO)**

LEIO is the interference of two beams. One is reflected from the surface (air/thin film) and the other is the PR signal reflected from the interface (thin film/substrate). Because the electric field is formed between the thin film layer and the substrate, we can measure the thin film layer thickness from the LEIO PR signals. The signal related to the variation in the refractive index of the substrate can be expressed as [3]:

\[
\frac{\Delta R}{R} = \frac{R(n_s n_s) - R(n_s n_s + \Delta n_s)}{R(n_s n_s)}, \tag{7a}
\]

\[
\Delta n_s = \frac{1}{4} (n_s^2 - 1) \frac{\Delta R_s}{R_s}, \tag{7b}
\]

where \( \Delta R_s/R_s \) is the PR signal of the substrate, \( \Delta n_s \) is the refractive index change of the substrate, and \( n_s \) and \( n_s \) are the refractive index of the thin film layer and the substrate, respectively. Equation (7b), which concerns the substrate refractive index variation and the refractive index change of the substrate, can be obtained simply using a reflection formula. By applying Eqs. (3) and (7) in the low electric field, the LEIO phenomenon occurring in the region below the fundamental bandgap, can be predicted.

Figure 2 shows the theoretical LEIO PR signal in the single GaSb layer. Using the theoretical model of \( \varepsilon_1 \) and \( \varepsilon_2 \) for III-V semiconductors developed by Adachi [13-15], we are able to directly calculate the Seraphin coefficients \( a \) and \( b \).

**III. Experimental details**

In this study, undoped-GaSb thin films were grown on \( n^+ \)-type GaSb (100) substrates doped with Te at a high concentration \((-10^{18} \text{ cm}^{-3})\). The growth temperature

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was approximately 485 °C. The GaSb thin film was grown to a thickness of 1 µm at a given substrate temperature with a Ga beam equivalent pressure (BEP) of $7 \times 10^{-7}$ Torr and a Sb$_4$ BEP of $5 \times 10^{-7}$ Torr. The samples after growth showed a stable Sb surface with a reflection high-energy electron diffraction pattern (1×3) at a given growth temperature. The crystal structure of the sample was evaluated by X-ray diffraction and the optical properties were evaluated by PR measurements at room temperature. For the PR measurements, a 1.3-µm laser diode was used as the modulation light source, with a modulation frequency of 800 Hz. The probe light was a beam obtained from a tungsten-halogen lamp (250 W) dispersed by a monochromator. The probe beam was incident on the sample surface, and the reflected beam was measured using an InGaAs detector. A closed-cycle He refrigerator was used to control the sample’s temperature.

### IV. Results and analysis

Figure 3 shows the PR signal and simulation results of the sample measured at room temperature. Owing to the decrease in the carrier concentration induced by increasing the growth temperature, the relative magnitude of the electric field is reduced. Table I shows the simulation results.

In the case of a thin film, the carrier concentration inside the sample is uniform and is depleted in the surface; therefore, the potential is changed in the inward direction. In this case, mainly the surface electric field is measured in the PR of the thin film sample, because the electric fields is related to the magnitude of the electric potential and the thickness of the surface depletion layer.

However, the experimental and simulation results show that the PR signals in the low and intermediate electric field region coexist. In general, the undoped-GaSb thin film grown on $n^+$-GaSb substrate exhibits p-type characteristics due to unintended natural defects and forms a p-n junction on the GaSb substrate. As a result, the PR signal in the low electric field region is formed at the undoped-GaSb thin film and the heavily doped substrate interface, and that in the intermediate electric field region appears at the undoped-GaSb surface.

The low-field PR signal is accompanied by the LEIO PR signal. The simulation results show that, with a growth temperature of 485 °C, the intermediate electric field is 70 kV/cm. Undoped-thin films and high doped substrates can be analyzed in the same way as p-n junctions. The thickness of the samples measured from the LEIO signals was $d = 1040$ nm. Due to the incident angle of the probe beam and the dispersion function of the medium, the measured thicknesses (1040 nm) and the production thicknesses (1000 nm) are slightly different.

### Table I. Theoretical parameters (Eqs. (3) and (5)) used to fit the experimental PR signal (Fig. 3). $m_{hh}$ and $m_l$ are the effective masses of heavy and light holes, respectively.

<table>
<thead>
<tr>
<th></th>
<th>$C$</th>
<th>$\phi$</th>
<th>$E_p$</th>
<th>$\Gamma_{sp}$</th>
<th>$m$</th>
<th>$\Delta_{hh}/\Delta_l$</th>
<th>$F$</th>
<th>$E_f$</th>
<th>$\Gamma$</th>
<th>$m_{hh}/m_l$</th>
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<td>TDFD</td>
<td>$2 \times 10^{-4}$</td>
<td>270</td>
<td>0.70</td>
<td>30</td>
<td>2.5</td>
<td></td>
<td></td>
<td></td>
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<tr>
<td>FKO</td>
<td>2.5/0.5</td>
<td>70</td>
<td>0.723</td>
<td>6</td>
<td>0.4/0.6</td>
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Figure 3. (Color online) (a) Experimental and theoretical PR signatures of GaSb at 300 K grown at 485 °C. (b) Theoretical PR signature decomposed into medium field PR (Airy), low field PR (TDFF), and LEIO. The fitting parameters used are shown in Table I.
V. Conclusions

In this study, undoped-GaSb layers were grown on high-concentration $n^+\text{GaSb}$ substrates at 485 °C by MBE. The experimental PR spectra of the sample were analyzed using theoretical approaches (TDFF, FKO, and LEIO). The theoretical simulation results were compared with experimental data to derive the electric field and thickness of the thin film layer formed at the interface between the undoped-GaSb thin film layer and the high-concentration GaSb substrate. In addition, the material’s properties, such as the effective mass of heavy (and light) holes and the broadening parameters, were confirmed.

Acknowledgments

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References